# AUDIO KEY FINDING USING FACEG: FUZZY ANALYSIS WITH THE CEG ALGORITHM

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Our key finding system consists of a series of O(n) realtime algorithms for determining key from polyphonic audio. The system comprises of two main parts as shown in Figure 1 [1]. The first part (the upper dashed box) generates pitch class information from audio using the standard FFT and a fuzzy analysis technique. The second component (the lower dashed box) uses the pitch class information to determine the key using Chew's Spiral Array model and Center of Effect Generator (CEG) key finding algorithm [2, 3]. A cleanup procedure uses key information to clarify the input

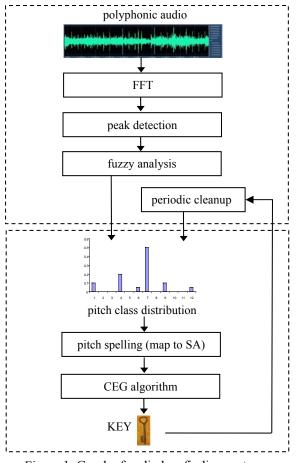


Figure 1. Graph of audio key finding system. distribution periodically.

#### **1 PITCH CLASS DETERMINATION**

The first component of the system consists of three steps for generating pitch class information from audio. We use the Fast Fourier Transform (FFT) to extract frequencies from audio wave signals. Then we employ a peak detection method to map frequencies to pitches. A fuzzy analysis technique is employed to improve the

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correctness of pitch class information using information on the overtone series.

We use the standard FFT to generate a frequency spectrum for each audio wave. We first define standard reference frequencies, from  $C_2$  to  $B_6$ , assuming that the pitch A above middle C is 440 Hz. The frequency range for each pitch is then bounded by the midpoints between its adjacent and its own reference frequencies. The peak detection method selects the maximum value within each frequency range using a heuristic based on the assumptions that a peak value is larger than the average values to its left and right, and that only one such maximum value exists. We use the maxima identified in the frequency ranges to construct the pitch class distribution. Details are provided in [4].

The fuzzy analysis technique improves the correctness of the pitch class distribution based on the overtone series. Because pitch frequencies are defined on a logarithmic scale, lower pitches produce more errors in mapping from frequency to pitches than higher ones. The fuzzy analysis technique uses the presence of the first overtones to clarify pitches of frequencies below 261 Hz (the pitch  $C_4$ ). More details are given in [1].

### 2 KEY FINDING FROM PITCH CLASS INFORMATION

Key assignment from pitch class information forms the second component of the system. We use Chew's Spiral Array model [2, 5] to represent the pitches in a 3-D space. The model forms the basis for both the key finding and the pitch spelling algorithms [6, 7]. We map the pitch class information from the previous part of the system to the Spiral Array model using the sliding window pitch spelling algorithm described in [7]; the CEG (Center of Effect Generator) key finding algorithm [3] is then used to determine the key.

The Spiral Array is a 3-dimensional model that represents pitches, intervals, chords, and keys in the same space for easy comparison. The pitches are shown as points on a helix, and adjacent pitches are related by intervals of perfect fifths, while vertical neighbors are related by major thirds. Central to the Spiral Array is the idea of the center of effect (CE), the representing of tonal objects as the weighted sum of their lower level components. In audio key finding, the CE is the sum of pitch points weighted by the pitch class distribution.

In the Center of Effect Generator (CEG) algorithm, key is determined by a nearest neighbor search among the major and minor key representations in the Spiral Array space. For short audio samples, the CEG algorithm progressively uses the cumulative pitch class information to determine the key. To eliminate excessive non-tonal noise that may have accumulated in the pitch class distribution, we introduce a periodic cleanup procedure. The cleanup process runs periodically, and uses the key results to zero-out the weights on pitch classes that are not in the key, and those that comprise the four smallest values among the 12 pitch classes.

The key finding system generates a key answer every 0.37 seconds using non-overlapping sliding windows. The pitch classes are assigned spellings whenever an answer is generated by the accumulated pitch class information from the previous 5 seconds. The cleanup procedure adjusts the pitch class distribution every 2.5 seconds.

The global key is computed using the cumulative pitch class information from the instance of the first non-silent signal to a pre-determined stopping point. The stopping point is determined as the point in time at which the training data achieves the highest percentage of correct key results. The stopping point we obtained from the training data is 13.32 seconds. That is to say, the desired global key is determined by the majority of the key answers for segments from the beginning to 13.32 seconds.

#### **3 EVALUATION RESULTS**

The evaluation was conducted using 1,252 audio files synthesized from two synthesizing software: Winamp and Timidity. The points for each key answer were assigned according to its relation to the ground truth (listed in Table 1). The composite score is calculated by averaging the Winamp and Timidity scores. Table 2 records the evaluation results for our system.

Table 1. Point assignments for key answers

	Correct	Perfect 5 <sup>th</sup>	Relative	Parallel	Others
Point	1	0.5	0.3	0.2	0

Table 2. Sur	nmary of the	evaluation results
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System and algorithms	Fuzzy analysis CEG algorithm with Spiral Array model	
Rank	7	
Composite percentage score	79.10%	
Synthesizer	Winamp	Timidity
Total score	1002.3	977.3
Percentage score	80.1%	78.1%
Correct keys	937	905
Perfect 5 <sup>th</sup> errors	83	95
Relative major/minor errors	66	68
Parallel major/minor errors	20	22
Other errors	146	162
Runtime (s)	3299	3468
Machine	OS:XP, Processor: Intel P4 3.0GHz, RAM:3GB	

#### **4** SYSTEM COMPARISONS

Six groups participated in the audio key finding contest for MIREX 2005, including Chuan & Chew, Gómez, İzmirl, Pauws, Purwins & Blankertz, and Zhu (listed alphabetically). In this section, we compare the known algorithms between proposed systems based on the short abstracts provided by, and made available to, all participants (first parts of [8, 9, 10, 11, 12]).

Table3-1. Summary of system comparisons

System proposed by	Chuan & Chew	Gómez	İzmirli
Sample window size	370ms	93ms	Unknown
Pitch extraction	FFT	FFT	FFT
Resolution	Semitone	1/3 semitone	Semitone
Audio character- istic analy- sis	Fuzzy analy- sis with peri- odic update	Modified K-S profile based	Combination K-S/T, with
Key templates	Key represen- tations in Spiral Array	on audio char- acteristics	weighted spec- tra profile
Query	CE in Spiral Array	НРСР	Chroma tem- plates
Key find- ing method	CEG	K-S (correla- tion)	K-S (correla- tion)
Selection criteria	Nearest key (Euclidena distance) at stopping point	Template with highest correla- tion coefficient at start or for entire file	Highest votes based on sum of correlation coefficients weighted by confidence values

Table3-2. Summary of system comparisons

System proposed by	Pauws	Purwins & Blankertz	Zhu
Sample window size	100ms	Unknown	Note onsets
Pitch extraction	FFT	Const-Q Trans- form	Const-Q Trans- form
Resolution	Semitone	1/3 semitone	1/2 semitone
Audio character- istic analy- sis	Chroma spectrum	Spectral leak- age effects	Pitch content is classified into mono, chord, and pitch sets
Key templates	Profiles from training data	Profiles from training data	Rules derived from training data
Query	Subharmonic summation	Constant quo- tient bins	Diatonic pitch classes
Key find- ing method	Some statisti- cal measure	Maximal corre- lation	Rule-based
Selection criteria	Unknown	The key with the maximal correlation in the first 15 seconds	Unknown

We list the each system's sample window size, pitch extraction technique, resolution, audio characteristic analysis method, key templates, query method, key finding method, and key selection criteria in Table 3-1 and 3-2.

From Table 3-1 and 3-2, we can see that the major differences between the systems are: audio characteristics analysis, key templates, and final selection criteria. The first two are sometimes combined in the design of the system. In Chuan & Chew's system, we use the key spirals as the pre-computed key templates. We used a fuzzy analysis technique to clarify the audio signals in order to generate more accurate pitch classes. In Gómez's system, the key templates are also precomputed; starting from the Krumhansl-Schmuckler pitch class profiles [13], she alters the profiles to take into account the chord and harmonics characteristic of audio signals. In İzmirli's, Pauws' and Purwins & Blankertz's systems, the key templates are constructed with audio characteristics. İzmirli creates the key templates from monotonic instrument sounds, weighted by a combination of the K-S and Temperley's modified profiles [14]. The key templates in Pauws' and Purwins & Blankertz's system are completely data-driven, that is to say, the parameters are learned from training data. In contrast, Zhu builds a rule-based key finding system in which the rules are learned from MIDI training data.

It is one matter to determine key, a feature that varies over time, but another to decide on which key to select as the "solution" when one must do so in a competition of this kind. We decided to use only a segment at the beginning of a test file. The best selection was determined to be the first 13.32 seconds of each piece, a parameter that yielded the most number of correct answers on the test set provided by the organizers. The reason for choosing a sample from only the beginning of the piece is that that is when the key is most likely to be established before modulating to other related keys. This assumption is validated by the results of Gómez's two system submissions. In the two versions of the system, the one using only the "start" portion of a piece performs better than the one employing the entire piece (labeled "global"). It is important to note that this assumption would not hold true for every piece.

The most effective selection criterion was proposed by İzmirli. His system tracks the confidence value for each key answer (a number based on the correlation coefficient between the query and key template), and the global key was selected as the one having the highest sum of confidence values over the length of the piece. The evaluation results demonstrate the importance of the selection criteria.

Apart from its selection criterion, we posit that Izmirli's system's winning performance in the audio key finding competition is due in part to his use of a combination of knowledge-driven (Temperley profiles), perceptually-supported (K-S profiles) and data-driven templates. Gómez's modified K-S profile, based on hypotheses of chord and harmonic effects, also works well, but it appears that theoretical propositions may not be as inclusive of audio-specific features as information learned from audio sounds. We used the Spiral Array's key representations (our key templates) without altering them to fit audio characteristics. The parameters for the original parameters for the key spiral were selected based on constraints derived from symbolic pitch and key relations.

In contrast, Pauws' method depends strongly on the representative ability of the training data. Both İzmirli's and Pauws' queries are pitch class distributions constructed in the frequency domain, rather than duration profiles, which may be a more appropriate measure when comparing to the FFT results. In both Gómez's and our approach, we compared some mapping of the duration profile or pitch positions weighted by durations to the key templates.

Distinct from other systems, we reconstruct the pitch class information from audio using a fuzzy analysis

technique, before applying the key finding algorithm. The reconstruction of pitch information explored the effect of audio properties such as the harmonics and frequency resolution of audio signals.

### **5** CONCLUSIONS

An advantage and disadvantage of our system is its lack of dependence on training data. Only the selection criterion (the stopping point) was determined from the sample test set. All other system parameters are predetermined, and unaffected by training data.

The key finding contest has allowed us to closely inspect and compare several key finding systems in close proximity. Our analysis of the systems and their performances reveal several avenues for improving ours. Improvements that can be made include:

• using a smaller audio sample window size, and separation of the analyses for low and high frequency audio signals;

• the calibrating of the Spiral Array models' parameters to take into account audio frequency features in the positioning of the key representations (templates), a technique similar to Gómez's and İzmirli's treatment of the K-S profiles; and,

• using distance of query from key representations to quantify the confidence of each key choice in order to obtain a more accurate selection of the most likely key.

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